

Search for Matter-Dependent Atmospheric Neutrino Oscillations in Super-Kamiokande

The Super-Kamiokande Collaboration

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We consider $\nu_\mu \rightarrow \nu_\tau$ oscillations in the context of the Mass Varying Neutrino (MaVaN) model, where the neutrino mass can vary depending on the electron density along the flight path of the neutrino. Our analysis assumes a mechanism with dependence only upon the electron density, hence ordinary matter density, of the medium through which the neutrino travels. Fully-contained, partially-contained and upward-going muon atmospheric neutrino data from the Super-Kamiokande detector, taken from the entire SK-I period of 1489 live days, are compared to MaVaN model predictions. We find that, for the case of 2-flavor oscillations, and for the specific models tested, oscillation independent of electron density is favored over density dependence. Assuming maximal mixing, the best-fit case and the density-independent case do not differ significantly.

I. INTRODUCTION

Neutrino oscillations result when at least one neutrino has mass different from the others, so that neutrinos mass eigenstates are distinct from the flavor eigenstates. For atmospheric neutrinos, $\nu_\mu \rightarrow \nu_\tau$ oscillations [1] are strongly favored over $\nu_\mu \rightarrow \nu_s$ oscillations [2] and other exotic mechanisms for neutrino disappearance [3]. Neutrino oscillation without the introduction of sterile flavors has also been sufficient to resolve the solar neutrino problem [4, 5].

Super-Kamiokande previously reported best fit parameters for atmospheric two-flavor $\nu_\mu \rightarrow \nu_\tau$ oscillations, providing an explanation of the atmospheric neutrino anomaly [6]. In Super-Kamiokande, where previous analyses always considered only geometric path length independent of medium, neutrino disappearance effects are strikingly evident for upward going neutrinos, which have passed through many km of rock, in comparison with downward-going neutrinos, which travel mainly through air. We note that other experiments that observed neutrino oscillations, such as KAMLAND [7], K2K [8], and MINOS [9], detected neutrinos whose path was almost entirely through rock.

Here we consider a possible consequence of the Mass Varying Neutrino (MaVaN) model [10]. In this model, the neutrino mass can vary depending on the matter density along the path of the neutrino. MaVaNs could provide a source for the dark energy [11]. Here we will assume that the mass variation of the neutrinos depends only upon the electron density of the environment, a possible side effect from radiative couplings of active neutrinos and electrons [10]. (In ordinary matter comprising the Earth's atmosphere and interior, overall matter density and baryon density, considered in other MaVaN scenarios, are essentially proportional to electron density.) If this hypothesis is accurate, it may be possible to probe the mass dependence with Super-Kamiokande data.

We used atmospheric neutrino data from the Super-Kamiokande-I running period (1996–2001) to test whether $\nu_\mu \rightarrow \nu_\tau$ oscillations have an apparent dependence on the electron density of the material the neutrino passes through. For this analysis, we assumed that the mass squared difference is proportional to some power of the electron density, $\Delta m_{eff}^2 \sim \rho^n$. We also assumed that the mixing angle is constant for all media.

II. DATA ANALYSIS

Super-Kamiokande is a water Cherenkov experiment located within Mt. Ikeno-yama in central Japan, under 2700 meters water equivalent rock overburden. It has a cylindrical design, holds 50 kilotons of water, and is divided into two optically separated sections by a structural framework that supports the photomultiplier tubes (PMTs). During the SK-I running period from which the data analyzed here came,

the detector had an inner detector (ID) equipped with 11146 50cm PMTs aimed inward, and an outer detector (OD) volume instrumented with 1885 20cm PMTs, aimed outward and equipped with wavelength-shifting plastic plates. The OD functions primarily as a veto counter, tagging charged particles that enter or exit the ID. Within the ID we define a central 22.5 kiloton fiducial volume, within which detector response is expected to be uniform. Fully-contained (FC) neutrino events are those where interaction products are observed in the ID, with no significant correlated activity in the OD, while partially-contained (PC) events are those where some interaction products exit the ID. Upward-going muon events are those where a penetrating particle travelling in the upward direction enters and either stops or passes through the detector, and are attributed to muons produced by neutrino interactions in the surrounding rock. In general terms, FC, PC, and upward muon events represent successively higher energy samples of neutrino interactions, ranging from 200 MeV for the lowest energy FC events to above 1 TeV for the highest energy upward-going muons. Further details regarding the Super-Kamiokande detector design, operation, calibrations, and data reduction can be found in [6, 12].

Super-Kamiokande-I (SK-I) data taking for physics analysis began on May 17, 1996 and lasted until a planned shut-down for refurbishing on July 16, 2001, including a total of 1489.2 days of effective livetime (92 kiloton-years) for FC and PC events, and 1645.9 days for upward-going muon events. The full Monte Carlo (MC) event sample generated for comparison is equivalent to a 100 live-year period. The SK-I database used in the analyses presented here has the following statistics: for FC events, 12180 data and 13676.7 MC events in a livetime-scaled sample, for PC events, 911 data and 1129.6 MC events. The upward-going muon statistics are: for stopping muon tracks (those that enter but do not exit the detector), 417.7 data and 713.5 MC events, and for through-going muon tracks, 1841.6 data and 1669.5 MC events, after background subtraction for near-horizontal downward-going muons as described in ref. [6].

Two different analyses are considered here. The first analysis does not take into account path length in air for neutrino oscillations. Instead, it assumes MaVaN-type oscillations only occur in high-density matter, taking into account surface, crust, mantle, and Earth core densities. In other words, the neutrino flight path length is in effect taken to be only that portion of the geometric path that lies in high density matter. Because the path length systematic error is not relevant in this test, it is removed from the list of 39 systematic errors that was used in previous Super-Kamiokande analyses. The second analysis also takes into account path length in air and its density in considering neutrino oscillations effects in the context of the MaVaN model.

A detailed description of the SK-I atmospheric neutrino chi-squared zenith angle analysis using the “pull” method [13] can be found in [6], and the same methods are applied here. A profile of the mountain surrounding Super-Kamiokande was

taken from topological maps to determine the downward neutrino path length in rock. The maps used are the United States Geological Survey agency's Digital Elevation Maps [14], with data points at 7.5 minute (about 30 meters) spacing.

In the conventional 2-flavor $\nu_\mu \rightarrow \nu_\tau$ oscillation framework, the oscillation probability can be written as

$$P(\nu_\mu \rightarrow \nu_\tau) = \sin^2 2\theta \sin^2 \left(\frac{1.27 \Delta m^2 L}{E_\nu} \frac{\text{GeV}}{\text{km} \cdot \text{eV}^2} \right),$$

where L is the distance travelled by the neutrino between production and detection, and E_ν is the neutrino energy, while the oscillation parameters are the mixing angle θ , and the mass difference squared, $\Delta m^2 = |m_2^2 - m_3^2|$ in the usual nomenclature. To test for density dependence, we replaced Δm^2 in the equation above with an effective mass difference that is proportional to the electron density of the medium, $\Delta m^2 \rightarrow \Delta m^2 \times \left(\frac{\rho_e}{\rho_0} \right)^n$, where ρ_e is the electron density of the matter in neutrino trajectory, and n parameterizes the density dependence. For neutrinos passing through layers of matter with different density, the path length in each layer is taken into account. ρ_0 is set at $6.02 \times 10^{23} \text{e/cm}^3$. Several different values of n are tested here, as described below. To approximate the mass density of the Earth for upward traveling neutrinos, the Preliminary Earth Reference Model (PREM) [15] is used. The electron density is taken to be the mass density multiplied by the charge-to-mass ratio [16].

Atmospheric neutrinos are produced at altitudes around 15 km above sea level. A neutrino travelling nearly vertically downward thus passes through about 15 km of air (low-density matter) followed by 1-2 km of rock (high density matter) before interacting within the detector, while a nearly-horizontal downward-going neutrino travels through over 200 km of air and about 10 km of rock. Thus, a downward neutrino has 8-20 times as much path length in air as in rock. If oscillation only occurs in high density matter, the effective path length will be shorter than the geometric path length travelled by the neutrino from point of production to detection. In that case, the standard oscillation model, which uses the full geometric path length, assumes more oscillation cycles occur for a given Δm^2 , and oscillation effects are more significant for neutrinos at low energies. Analyses both including, and neglecting, the air path length are considered here.

A. Analysis Neglecting Air path length

Density dependent oscillation models were first tested neglecting the air path length and using specified values of n suggested by theorists [17]. The results are shown in Table I for two cases: fits constrained to lie in the physical region, where maximal mixing is assumed for all densities, and with this constraint relaxed, where mixing angle is allowed to vary. All models tested are ruled out, with confidence level better than 99.9%, when compared to fits assuming oscillations independent of density of the medium (including air).

Next, we treat the density dependence as a free parameter, and find the best fit electron density dependence exponent n

for the case of matter-dependent oscillations assuming maximal mixing ($\sin^2(2\theta) = 1$) in all densities (except air). This analysis uses both n and Δm^2 as the varied parameters. Δm^2 values from 10^{-4} to 10^0eV^2 were used over 81 bins, and density dependence powers from $n = -3$ to $+3$ were considered, over 61 bins. The results produce a $\chi^2_{\min} = 187.3/178$ d.o.f. for $(n, \Delta m^2) = (-0.30, 3.16 \times 10^{-3} \text{eV}^2)$. Thus, the model in which air path length is neglected, *i.e.*, oscillations occur only in rock, is disfavored at about the 3.5σ level relative to standard oscillations.

B. Analysis Including Air path length

We repeated the analysis, this time taking into account the path length in air. Now the $n = 0$ case, where there is no dependence on the electron density, corresponds to the conventional oscillations model, since the full geometric path length is used.

The air mass density depends greatly on the altitude of the air above sea level. For simplicity, a constant value of 10^{-3}g/cm^3 (corresponding to actual air density at mountain altitude) was used for the mass density.

The same set of fixed n values are tested again, to check various density dependences, this time including the air path length. The results are listed in Table II. All models tested are excluded by $\geq 3.8\sigma$ when compared to the density-independent case.

Finally, we again treat density dependence n as a free parameter, this time taking air path length into account, once more assuming maximal mixing. The results are shown in Figure 1. A minimum $\chi^2 = 174.3/178$ d.o.f. is found at $(n, \Delta m^2) = (-0.04, 1.95 \times 10^{-3} \text{eV}^2)$. This result and the standard 2-flavor oscillation result (*i.e.* with $n \equiv 0$) do not differ significantly.

III. SUMMARY AND CONCLUSIONS

We used data from Super-Kamiokande-I to test mass-varying neutrino models, by considering oscillation effects where the effective mass of a neutrino is dependent on the matter environment of the neutrino flight path. Our analysis assumed varying neutrino mass was due entirely to the electron density of the material in a neutrino's path, a possible consequence of the MaVaN theory. Assuming a constant mixing angle in all environments, we substituted Δm^2 with $\Delta m^2 \times \left(\frac{\rho_e}{\rho_0} \right)^n$ (where $\rho_0 = 6.02 \times 10^{23} \text{e/cm}^3$) for specific values of n suggested by theorists, as well as with n as a fitted parameter. Two different models were considered. In the first analysis, we neglected the portion of the neutrino flight path in low density matter (air), and assumed mass-varying effects occur only in high density matter (rock). For the second analysis, we allowed oscillation effects in all portions of the neutrino path, but (in contrast to the conventional oscillation analysis, where only the geometric path length is considered) took into account mass densities. The primary difference in the two

TABLE I: Comparisons of χ^2 Values for different models without air path. There are a total of 178 degrees of freedom in the χ^2 (see ref. [6]). Note that $n = 0$ is *not* equivalent to oscillations independent of medium, because here we do not allow for any oscillations in air.

Model $\Delta m^2 \times (\rho/\rho_o)^n$	Physical Region				Unphysical Region		
	χ^2_{min}	$\Delta m^2(\text{eV}^2)$	$\sin^2(2\theta)$	$\Delta\sigma$	χ^2_{min}	$\Delta m^2(\text{eV}^2)$	$\sin^2(2\theta)$
$n = 2$	203.4	4.84×10^{-4}	1.00	5.3	203.1	4.67×10^{-4}	1.02
$n = 1$	194.7	1.12×10^{-3}	1.00	4.4	194.1	1.19×10^{-3}	1.04
$n = \frac{2}{3}$	192.5	1.46×10^{-3}	1.00	4.2	191.7	1.46×10^{-3}	1.04
$n = \frac{1}{3}$	190.5	1.60×10^{-3}	1.00	3.9	189.5	1.60×10^{-3}	1.04
$n = 0$	189.8	2.66×10^{-3}	1.00	3.8	188.9	2.66×10^{-3}	1.04
$n = -\frac{1}{3}$	188.5	3.16×10^{-3}	1.00	3.7	187.5	2.92×10^{-3}	1.04
$n = -\frac{2}{3}$	187.9	3.12×10^{-3}	1.00	3.6	187.0	3.12×10^{-3}	1.04
$n = -1$	188.5	3.80×10^{-3}	1.00	3.7	187.6	3.80×10^{-3}	1.04
$n = -2$	190.1	4.73×10^{-3}	1.00	3.9	188.7	4.73×10^{-3}	1.05

TABLE II: Comparisons of χ^2 Values for Different Models including air path. Note that here, $n = 0$ is equivalent to oscillations independent of medium.

Model $\Delta m^2 \times (\rho/\rho_o)^n$	Physical Region				Unphysical Region		
	χ^2_{min}	$\Delta m^2(\text{eV}^2)$	$\sin^2(2\theta)$	$\Delta\sigma$	χ^2_{min}	$\Delta m^2(\text{eV}^2)$	$\sin^2(2\theta)$
Equal medium oscillations ($n=0$)	175.0	2.11×10^{-3}	1.00	-	174.7	2.11×10^{-3}	1.02
$n = 2$	203.4	4.84×10^{-4}	1.02	5.3	203.1	4.67×10^{-4}	1.00
$n = 1$	194.7	1.12×10^{-3}	1.00	4.4	194.1	1.12×10^{-3}	1.04
$n = \frac{2}{3}$	192.4	1.46×10^{-3}	1.00	4.2	191.7	1.46×10^{-3}	1.04
$n = \frac{1}{3}$	189.6	1.60×10^{-3}	1.00	3.8	188.7	1.60×10^{-3}	1.04
$n = -\frac{1}{3}$	228.5	7.50×10^{-4}	0.91	7.9	228.5	7.50×10^{-4}	0.91
$n = -\frac{2}{3}$	392.1	1.50×10^{-4}	0.63	14.7	392.1	1.50×10^{-4}	0.70
$n = -1$	447.8	3.63×10^{-2}	0.60	16.5	447.8	3.63×10^{-2}	0.60
$n = -2$	447.9	3.73×10^{-3}	0.60	16.5	447.9	3.73×10^{-3}	0.60

hypothesis lies in the effective path lengths for near-horizontal downward-going neutrinos.

In the “pull” fitting procedure used, some of the systematic errors are allowed to vary in the fit. When fitted systematics are forced significantly outside a reasonable range of values, it is an indication that the model used is disfavored by the data. For the high-density-only oscillation model, some of the systematics, particularly the ν_μ/ν_e ratio for energies below 5 GeV, adjusted to values beyond a reasonable deviation from the expected value. This does not happen when fitting to the conventional oscillation model, and results in a larger chi-squared value for the mass-dependent models. Based on relative chi-squared values in our results, the hypothesis that neutrinos oscillate only in high density matter is disfavored relative to conventional oscillations by at least 3.5 σ , without requiring additional effects.

For the second analysis, where oscillations in low density matter were included, a mass difference with electron density dependence is disfavored at more than the 3.8- σ level when compared with neutrino oscillations with a fixed mass difference, for all fixed values of n tested. In addition, a freely varying density dependence analysis was performed, assuming maximal mixing. It produced a minimum chi-

squared value of $\chi^2_{min} = 174.3/178$ d.o.f. at ($n = -0.04, \Delta m^2 = 1.95 \times 10^{-3} \text{eV}^2$), consistent (within 1.4 σ) with the $n = 0$ (no density dependence) case.

The results of our analyses show no evidence that the environmental electron density influences the effective Δm^2 determined using Super-Kamiokande atmospheric neutrino data. We have not explicitly considered models where the mixing angle is not constant in all densities, or which assume 3 flavor oscillations, nor do we exclude all variations of MaVaN models. We find that conventional density independent $\nu_\mu \rightarrow \nu_\tau$ oscillations are sufficient to explain the atmospheric neutrino data.

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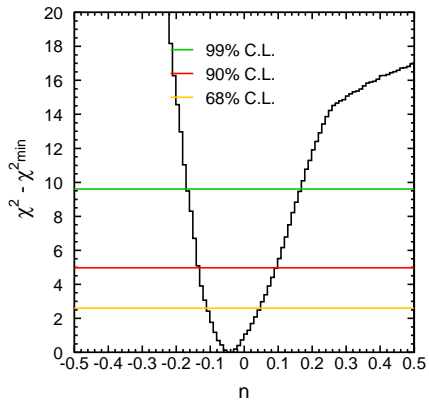
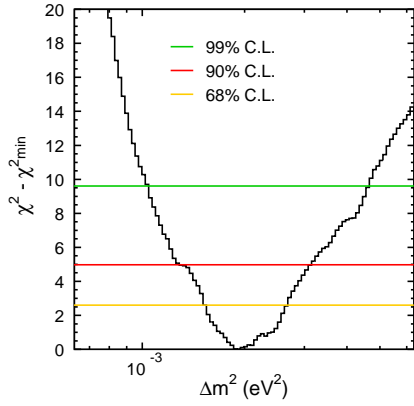
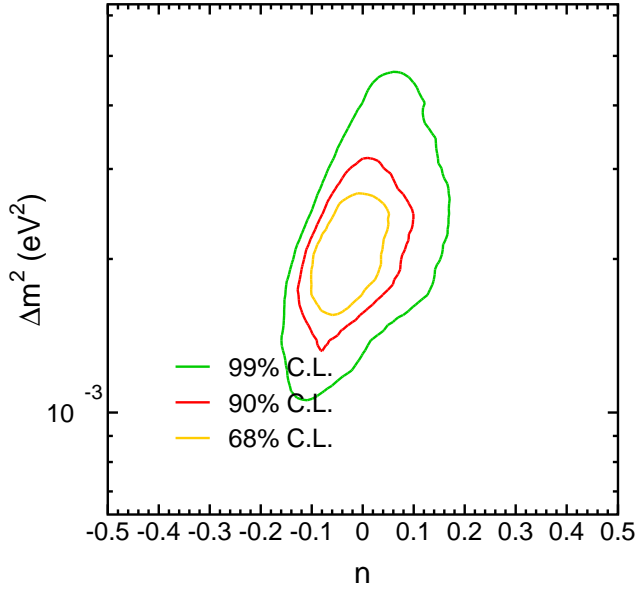


FIG. 1: $\Delta m^2 \rightarrow \Delta m^2 \times \left(\frac{\rho_c}{\rho_o}\right)^n$ (including air path length). Upper plot shows relative- χ^2 confidence level contours on the Δm^2 versus n plane, obtained when taking into account both high and low density matter path lengths. The lower plots display the $\chi^2 - \chi^2_{\min}$ contours, with confidence levels shown, at the best-fit parameter values.